

M2 NPAC — From Nuclei to Stars

Phenomenological aspects : mid-term exam

November 16th 2018

1 Course questions

Question 1

- (a) Remind the definitions of the following quantities: b , p , p_+ , p_- , $g_+ = p_+/p$ and $g_- = p_-/p$.
- (b) Explain how a nuclear interaction with exchange character leads to the observed saturation properties of nuclear matter (use quantities b , p , p_+ , p_- , $g_+ = p_+/p$ and $g_- = p_-/p$ previously defined and the relative distance between nucleons).
- (c) What are the nuclear properties which show saturation?
- (d) Give the expression of the nuclear radius in normal saturation condition as a function of A (the number of nucleons) and b , explain how the expression is obtained from considerations in (b) above.

Question 2

- (a) What are the two parameters of the liquid drop model mass formula that shape the valley of stability, explain qualitatively why.
- (b) What are the two parameters of the liquid drop model mass formula that define the end of the valley of stability towards large A and Z , explain qualitatively why.

Question 3

- (a) Draw the normal partitions for nuclei with mass $A = 14$, from $Z = 5$ to $Z = 9$ (included). Give isospin and partition numbers (P, P', P'') for each case.
- (b) Draw the mass parabola for this chain in a way similar to slide n°21 in slide set n°1. Explain what happens at isospin number 0.

Turn the page.

2 Problem

In 1966 Garvey and Kelson [Physical Review Letters 16, 197 (1966)] put forward a new mass relationship suitable to predict the drip line with higher precision than the liquid drop formula can do. The mass relationship is:

$$M(N + 2, Z - 2) - M(N, Z) = M(N + 1, Z - 2) - M(N, Z - 1) + M(N + 2, Z - 1) - M(N + 1, Z). \quad (1)$$

The authors justified this mass relationship with the following figure:

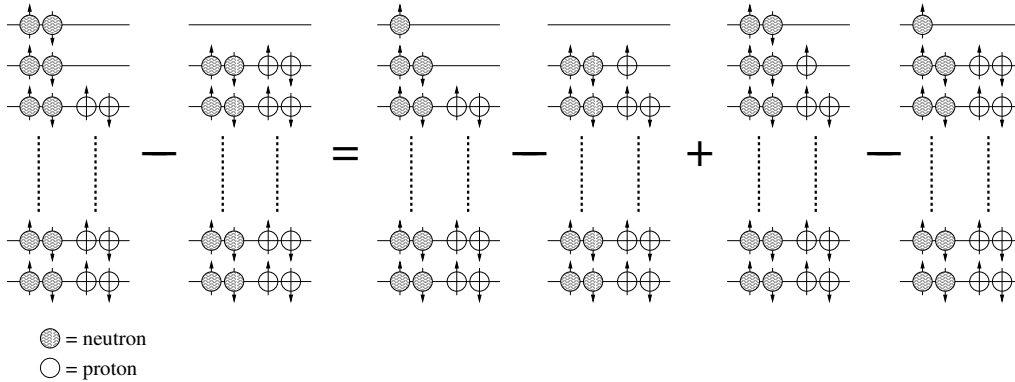


Fig. 1

Question 4

Show that this equation is correct from the point of view of the symmetry energy up to a certain approximation, give this approximation. **Hint** Use partition numbering (P, P', P'').

The authors say that the formula can be used for any A provided that:
“ N must be equal to or greater than Z and if $N = Z$ they must *not* be odd”

Question 5

Justify the reason why if $N = Z$, N and Z must *not* be odd.

Question 6

- Predict the mass excess of ^{16}C using the extraction of the evaluated mass table given next page. Compare to the experimental tabulated value of ^{16}C .
- Give a possible reason for the difference observed.