

Exercise sheet № 7 - W boson properties

1 W-boson mass measurement

We consider the production of the W boson in $p\bar{p}$ collisions, with the proton beam oriented along the \vec{z} axis. We assume that at first order the W boson is emitted with $p_T^W \approx 0$.

1. We first consider the hadronic decay of the W . While the W -boson invariant mass can be fully reconstructed, give at least two reasons which makes the measurement in this channel extremely challenging.
2. We then consider the leptonic decay $W \rightarrow \ell\nu$ with $\ell \equiv e, \mu$. Draw the 2 Feynman diagrams of the productions and decay.
3. In this case, the lepton energy is extremely well measured. What makes the measurement of the mass peak impossible ?
4. We consider only the $u\bar{d}$ production and we note θ^* the angle between the positron and the beam axis in the center-of-mass (CM) frame. What is the distribution in this frame of differential cross section $d\sigma/d\cos\theta^*$ (see the course or in the exercise sheet 7 for a detailed demonstration).
5. In the center of mass, write p_T^e as a function of the $\cos^2\theta^*$ using the fact that $m_e, m_\nu \ll m_W$.
6. Write $d\sigma/dp_T^e$ as a function of p_T^e , and $d\sigma/d\cos\theta^*$.
7. What is the peculiarity of this distribution that allows to make a measurement of the m_W ?

2 W-boson branching ratios

In this exercise we define $\Gamma_\ell \equiv \Gamma(W^- \rightarrow e^-\bar{\nu}_e)$ and

1. As a function of Γ_ℓ , give the values of $\Gamma(W^- \rightarrow \mu^-\bar{\nu}_\mu)$ and $\Gamma(W^- \rightarrow \tau^-\bar{\nu}_\tau)$.
2. As a function of Γ_ℓ , give the values of $\Gamma(W^- \rightarrow \bar{u}d')$, $\Gamma(W^- \rightarrow \bar{c}s')$ and $\Gamma(W^- \rightarrow \bar{t}b')$.
3. Conclude on the value of $\mathcal{B}(W^- \rightarrow e^-\bar{\nu}_e)$ and compare to the value found in the PDG.